

5. $\sin x = \frac{5}{13}$, $\operatorname{cosec} x = \frac{13}{5}$, $\cos x = -\frac{12}{13}$, $\sec x = -\frac{13}{12}$, $\cot x = -\frac{12}{5}$

6. $\frac{1}{\sqrt{2}}$

7. 2

8. $\sqrt{3}$

9. $\frac{\sqrt{3}}{2}$

10. 1

EXERCISE 3.3

5. (i) $\frac{\sqrt{3}+1}{2\sqrt{2}}$ (ii) $2 - \sqrt{3}$

EXERCISE 3.4

1. $\frac{\pi}{3}, \frac{4\pi}{3}, n\pi + \frac{\pi}{3}, n \in \mathbf{Z}$

2. $\frac{\pi}{3}, \frac{5\pi}{3}, 2n\pi \pm \frac{\pi}{3}, n \in \mathbf{Z}$

3. $\frac{5\pi}{6}, \frac{11\pi}{6}, n\pi + \frac{5\pi}{6}, n \in \mathbf{Z}$

4. $\frac{7\pi}{6}, \frac{11\pi}{6}, n\pi + (-1)^n \frac{7\pi}{6}, n \in \mathbf{Z}$

5. $x = \frac{n\pi}{3}$ or $x = n\pi, n \in \mathbf{Z}$

6. $x = (2n+1)\frac{\pi}{4}$, or $2n\pi \pm \frac{\pi}{3}, n \in \mathbf{Z}$

7. $x = n\pi + (-1)^n \frac{7\pi}{6}$ or $(2n+1)\frac{\pi}{2}, n \in \mathbf{Z}$

8. $x = \frac{n\pi}{2}$, or $\frac{n\pi}{2} + \frac{3\pi}{8}, n \in \mathbf{Z}$

9. $x = \frac{n\pi}{3}$, or $n\pi \pm \frac{\pi}{3}, n \in \mathbf{Z}$

Miscellaneous Exercise on Chapter 3

8. $\frac{2\sqrt{5}}{5}, \frac{\sqrt{5}}{5}, \frac{1}{2}$

9. $\frac{\sqrt{6}}{3}, -\frac{\sqrt{3}}{3}, -\sqrt{2}$

10. $\frac{\sqrt{8+2\sqrt{15}}}{4}, \frac{\sqrt{8-2\sqrt{15}}}{4}, 4+\sqrt{15}$

EXERCISE 5.1

1. $3 + i0$

2. $0 + i0$

3. $0+i1$

4. $14 + 28i$

5. $2 - 7i$

6. $-\frac{19}{5} - \frac{21i}{10}$

7. $\frac{17}{3} + i\frac{5}{3}$

8. $-4 + i0$

9. $-\frac{242}{27} - 26i$

10. $\frac{-22}{3} - i\frac{107}{27}$

11. $\frac{4}{25} + i\frac{3}{25}$

12. $\frac{\sqrt{5}}{14} - i\frac{3}{14}$

13. $0 + i1$

14. $0 - i\frac{7\sqrt{2}}{2}$

EXERCISE 5.2

1. $2, -\frac{2\pi}{3}$

2. $2, \frac{5\pi}{6}$

3. $\sqrt{2}\left(\cos\frac{-\pi}{4} + i\sin\frac{-\pi}{4}\right)$

4. $\sqrt{2}\left(\cos\frac{3\pi}{4} + i\sin\frac{3\pi}{4}\right)$

5. $\sqrt{2}\left(\cos\frac{-3\pi}{4} + i\sin\frac{-3\pi}{4}\right)$

6. $3(\cos\pi + i\sin\pi)$

7. $2\left(\cos\frac{\pi}{6} + i\sin\frac{\pi}{6}\right)$

8. $\cos\frac{\pi}{2} + i\sin\frac{\pi}{2}$

EXERCISE 5.3

1. $\pm\sqrt{3}i$

2. $\frac{-1 \pm \sqrt{7}i}{4}$

3. $\frac{-3 \pm 3\sqrt{3}i}{2}$

4. $\frac{-1 \pm \sqrt{7}i}{-2}$

5. $\frac{-3 \pm \sqrt{11}i}{2}$

6. $\frac{1 \pm \sqrt{7}i}{2}$

7. $\frac{-1 \pm \sqrt{7}i}{2\sqrt{2}}$

8. $\frac{\sqrt{2} \pm \sqrt{34}i}{2\sqrt{3}}$

9. $\frac{-1 \pm \sqrt{(2\sqrt{2}-1)i}}{2}$

10. $\frac{-1 \pm \sqrt{7}i}{2\sqrt{2}}$