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5.37 For the coin to revolve with the disc, the force of friction should be enough to provide the necessary centripetal force, i.e $\frac{mv^2}{r} \le \mu \, m \, g$. Now $v = r\omega$, where $\omega = \frac{2\pi}{T}$ is the angular frequency of the disc. For a given μ and ω , the condition is $r \le \mu g / \omega^2$. The condition is satisfied by the nearer coin (4 cm from the centre).

- 5.38 At the uppermost point, $N + mg = \frac{mv^2}{R}$, where N is the normal force (downwards) on the motorcyclist by the ceiling of the chamber. The minimum possible speed at the uppermost point corresponds to N = 0. i.e. $v_{\min} = \sqrt{Rg} = \sqrt{25 \times 10} = 16 \, \text{m s}^{-1}$
- The horizontal force N by the wall on the man provides the needed centripetal force : $N = mR \omega^2$. The frictional force f (vertically upwards) opposes the weight mg. The man remains stuck to the wall after the floor is removed if $mg = f < \mu N$ i.e. $mg < \mu mR \omega^2$. The minimum angular speed of rotation of the cylinder is $\omega_{min} = \sqrt{g/\mu R} = 5 \text{ s}^{-1}$
- 5.40 Consider the free-body diagram of the bead when the radius vector joining the centre of the wire makes an angle θ with the vertical downward direction. We have $mg = N\cos\theta$ and $mR\sin\theta$ $\omega^2 = N\sin\theta$. These equations give $\cos\theta = g/R\omega^2$. Since $\cos\theta \le 1$,

the bead remains at its lowermost point for $\omega \leq \sqrt{\frac{g}{R}}$

For
$$\omega = \sqrt{\frac{2g}{R}}$$
, $\cos \theta = \frac{1}{2}$ i.e. $\theta = 60^{\circ}$.

Chapter 6

- **6.1** (a) +ve (b) -ve (c) -ve (d) + ve (e) ve
- 6.2 (a) 882 J; (b) -247 J; (c) 635 J; (d) 635 J; Work done by the net force on a body equals change in its kinetic energy.
- 6.3 (a) x > a; 0 (c) x < a, x > b; V_1 (b) $-\infty < x < \infty$; V_1 (d) b/2 < x < -a/2, a/2 < x < b/2; - V_1
- (a) rocket; (b) For a conservative force work done over a path is minus of change in potential energy. Over a complete orbit, there is no change in potential energy; (c) K.E. increases, but P.E. decreases, and the sum decreases due to dissipation against friction; (d) in the second case.
- 6.6 (a) decrease; (b) kinetic energy; (c) external force; (d) total linear momentum, and also total energy (if the system of two bodies is isolated).
- **6.7** (a) F; (b) F; (c) F; (d) F (true usually but not always, why?)
- **6.8** (a) No
 - (b) Yes
 - (c) Linear momentum is conserved during an inelastic collision, kinetic energy is, of course, not conserved even after the collision is over.
 - (d) elastic.
- **6.9** (b) t

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- **6.10** (c) $t^{3/2}$
- 6.11 12 J
- **6.12** The electron is faster, $v_e/v_p = 13.5$
- **6.13** $0.082 \, \text{J}$ in each half; $-0.163 \, \text{J}$
- 6.14 Yes, momentum of the molecule + wall system is conserved. The wall has a recoil momentum such that the momentum of the wall + momentum of the outgoing molecule equals momentum of the incoming molecule, assuming the wall to be stationary initially. However, the recoil momentum produces negligible velocity because of the large mass of the wall. Since kinetic energy is also conserved, the collision is elastic.
- 6.15 43.6 kW
- **6.16** (b)
- **6.17** It transfers its entire momentum to the ball on the table, and does not rise at all.
- **6.18** 5.3 m s⁻¹
- **6.19** 27 km h^{-1} (no change in speed)
- **6.20** 50 J
- **6.21** (a) $m = \rho A v t$ (b) $K = \rho A v^3 t / 2$ (c) P = 4.5 kW
- **6.22** (a) $49,000 \,\mathrm{J}$ (b) $6.45 \,10^{-3} \,\mathrm{kg}$
- **6.23** (a) 200 m²(b) comparable to the roof of a large house of dimension $14m \times 14m$.
- **6.24** 21.2 cm, 28.5 J
- No, the stone on the steep plane reaches the bottom earlier; yes, they reach with the same speed v, [since $mgh = (1/2) m v^2$]

$$v_{\scriptscriptstyle B} = v_{\scriptscriptstyle C} = 14.1~{\rm m~s^{\scriptscriptstyle -1}}$$
 , $t_{\scriptscriptstyle B} = 2\sqrt{2}~{\rm s}$, $~t_{\scriptscriptstyle C} = 2\sqrt{2}~{\rm s}$

- **6.26** 0.125
- **6.27** 8.82 J for both cases.
- **6.28** The child gives an impulse to the trolley at the start and then runs with a constant relative velocity of 4 m s⁻¹ with respect to the trolley's new velocity. Apply momentum conservation for an observer outside. 10.36 m s^{-1} , 25.9 m.
- **6.29** All except (V) are impossible.

Chapter 7

- 7.1 The geometrical centre of each. No, the CM may lie outside the body, as in case of a ring, a hollow sphere, a hollow cylinder, a hollow cube etc.
- 7.2 Located on the line joining H and C1 nuclei at a distance of 1.24 Å from the H end.
- 7.3 The speed of the CM of the (trolley + child) system remains unchanged (equal to v) because no external force acts on the system. The forces involved in running on the trolley are internal to this system.
- 7.6 $l_z = xp_y yp_x$, $l_x = yp_z zp_y$, $l_y = zp_x xp_z$
- **7.8** 72 cm
- 7.9 3675 N on each front wheel, 5145 N on each back wheel.
- **7.10** (a) 7/5 MR² (b) 3/2 MR²