

- 4.17**  $9.9 \text{ m s}^{-2}$ , along the radius at every point towards the centre.
- 4.18**  $6.4 \text{ g}$
- 4.19** (a) False (true only for uniform circular motion)  
(b) True, (c) True.
- 4.20** (a)  $\mathbf{v}(t) = (3.0 \hat{\mathbf{i}} - 4.0t \hat{\mathbf{j}})$   $\mathbf{a}(t) = -4.0 \hat{\mathbf{j}}$   
(b)  $8.54 \text{ m s}^{-1}$ ,  $70^\circ$  with  $x$ -axis.
- 4.21** (a)  $2 \text{ s}$ ,  $24 \text{ m}$ ,  $21.26 \text{ m s}^{-1}$
- 4.22**  $\sqrt{2}$ ,  $45^\circ$  with the  $x$ -axis;  $\sqrt{2}$ ,  $-45^\circ$  with the  $x$ -axis,  $(5/\sqrt{2}, -1/\sqrt{2})$ .
- 4.23** (b) and (e)
- 4.24** Only (e) is true
- 4.25**  $182 \text{ m s}^{-1}$
- 4.27** No. Rotations in *general* cannot be associated with vectors
- 4.28** A vector can be associated with a plane area
- 4.29** No
- 4.30** At an angle of  $\sin^{-1}(1/3) = 19.5^\circ$  with the vertical;  $16 \text{ km}$ .
- 4.31**  $0.86 \text{ m s}^{-2}$ ,  $54.5^\circ$  with the direction of velocity

## Chapter 5

- 5.1** (a) to (d) No net force according to the First Law  
(e) No force, since it is far away from all material agencies producing electromagnetic and gravitational forces.
- 5.2** The only force in each case is the force of gravity, (neglecting effects of air) equal to  $0.5 \text{ N}$  vertically downward. The answers do not change, even if the motion of the pebble is not along the vertical. The pebble is not at rest at the highest point. It has a constant horizontal component of velocity throughout its motion.
- 5.3** (a)  $1 \text{ N}$  vertically downwards (b) same as in (a)  
(c) same as in (a); force at an instant depends on the situation at that instant, not on history.  
(d)  $0.1 \text{ N}$  in the direction of motion of the train.
- 5.4** (i) T
- 5.5**  $a = -2.5 \text{ m s}^{-2}$ . Using  $v = u + at$ ,  $0 = 15 - 2.5t$  i.e.,  $t = 6.0 \text{ s}$
- 5.6**  $a = 1.5/25 = 0.06 \text{ m s}^{-2}$   
 $F = 3 \times 0.06 = 0.18 \text{ N}$  in the direction of motion.
- 5.7** Resultant force =  $10 \text{ N}$  at an angle of  $\tan^{-1}(3/4) = 37^\circ$  with the direction of  $8 \text{ N}$  force.  
Acceleration =  $2 \text{ m s}^{-2}$  in the direction of the resultant force.
- 5.8**  $a = -2.5 \text{ m s}^{-2}$ , Retarding force =  $465 \times 2.5 = 1.2 \times 10^3 \text{ N}$
- 5.9**  $F - 20,000 \times 10 = 20000 \times 5.0$ , i.e.,  $F = 3.0 \times 10^5 \text{ N}$
- 5.10**  $a = -20 \text{ m s}^{-2}$   $0 \leq t \leq 30 \text{ s}$

$$t = -5 \text{ s} : x = u t = -10 \times 5 = -50 \text{ m}$$

$$t = 25 \text{ s} : x = u t + \frac{1}{2} a t^2 = (10 \times 25 - 10 \times 625) \text{ m} = -6 \text{ km}$$

$t = 100 \text{ s}$  : First consider motion up to 30 s

$$x_1 = 10 \times 30 - 10 \times 900 = -8700 \text{ m}$$

$$\text{At } t = 30 \text{ s, } v = 10 - 20 \times 30 = -590 \text{ m s}^{-1}$$

$$\text{For motion from 30 s to 100 s: } x_2 = -590 \times 70 = -41300 \text{ m}$$

$$x = x_1 + x_2 = -50 \text{ km}$$

**5.11** (a) Velocity of car (at  $t = 10 \text{ s}$ )  $= 0 + 2 \times 10 = 20 \text{ m s}^{-1}$

By the First Law, the horizontal component of velocity is  $20 \text{ m s}^{-1}$  throughout.

Vertical component of velocity (at  $t = 11 \text{ s}$ )  $= 0 + 10 \times 1 = 10 \text{ m s}^{-1}$

Velocity of stone (at  $t = 11 \text{ s}$ )  $= \sqrt{20^2 + 10^2} = \sqrt{500} = 22.4 \text{ m s}^{-1}$  at an angle of  $\tan^{-1}(\frac{1}{2})$  with the horizontal.

(b)  $10 \text{ m s}^{-2}$  vertically downwards.

**5.12** (a) At the extreme position, the speed of the bob is zero. If the string is cut, it will fall vertically downwards.

(b) At the mean position, the bob has a horizontal velocity. If the string is cut, it will fall along a parabolic path.

**5.13** The reading on the scale is a measure of the force on the floor by the man. By the Third Law, this is equal and opposite to the normal force  $N$  on the man by the floor.

(a)  $N = 70 \times 10 = 700 \text{ N}$ ; Reading is 70 kg

(b)  $70 \times 10 - N = 70 \times 5$ ; Reading is 35 kg

(c)  $N - 70 \times 10 = 70 \times 5$ ; Reading is 105 kg

(d)  $70 \times 10 - N = 70 \times 10$ ; Reading would be zero; the scale would read zero.

**5.14** (a) In all the three intervals, acceleration and, therefore, force are zero.

(b)  $3 \text{ kg m s}^{-1}$  at  $t = 0$ ; (c)  $-3 \text{ kg m s}^{-1}$  at  $t = 4 \text{ s}$ .

**5.15** If the 20 kg mass is pulled,

$$600 - T = 20 a, \quad T = 10 a$$

$$a = 20 \text{ m s}^{-2}, \quad T = 200 \text{ N}$$

If the 10 kg mass is pulled,  $a = 20 \text{ m s}^{-2}$ ,  $T = 400 \text{ N}$

**5.16**  $T - 8 \times 10 = 8 a, 12 \times 10 - T = 12 a$

i.e.  $a = 2 \text{ m s}^{-2}$ ,  $T = 96 \text{ N}$

**5.17** By momentum conservation principle, total final momentum is zero. Two momentum vectors cannot sum to a null momentum unless they are equal and opposite.

**5.18** Impulse on each ball  $= 0.05 \times 12 = 0.6 \text{ kg m s}^{-1}$  in magnitude. The two impulses are opposite in direction.

**5.19** Use momentum conservation:  $100 v = 0.02 \times 80$

$$v = 0.016 \text{ m s}^{-1} = 1.6 \text{ cm s}^{-1}$$

**5.20** Impulse is directed along the bisector of the initial and final directions. Its magnitude is  $0.15 \times 2 \times 15 \times \cos 22.5^\circ = 4.2 \text{ kg m s}^{-1}$

**5.21**  $v = 2\pi \times 1.5 \times \frac{40}{60} = 2\pi \text{ m s}^{-1}$

$$T = \frac{mv^2}{R} = \frac{0.25 \times 4\pi^2}{1.5} = 6.6 \text{ N}$$